

Influence of defect thickness on the angular dependence of coercivity in rare-earth permanent magnets

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The coercive field and angular dependence of the coercive field of single-grain $\text{Nd}_2\text{Fe}_{14}\text{B}$ permanent magnets are computed using finite element micromagnetics. It is shown that the thickness of surface defects plays a critical role in determining the reversal process. For small defect thicknesses reversal is heavily driven by nucleation, whereas with increasing defect thickness domain wall de-pinning becomes more important. This change results in an observable shift between two well-known behavioral models.

A similar trend is observed in experimental measurements of bulk samples, where a Nd-Cu infiltration process has been used to enhance coercivity by modifying the grain boundaries. When account is taken of the imperfect grain alignment of real magnets, the single-grain computed results appears to closely match experimental behaviour.

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The reduced value of the coercive field seen experimentally in rare-earth permanent magnets with respect to the Stoner-Wohlfarth coherent rotation value¹, may be related to the fact that a defect layer with reduced anisotropy exists at the surface of Nd₂Fe₁₄B²⁻⁴. This has been examined by Kronmüller and collaborators, within the so-called analytical micro-magnetic model^{2,3}. From comparison between model predictions and experimental data, it was concluded that Stoner-Wohlfarth “true nucleation” at defects governs the demagnetization processes³. The analysis of the temperature dependences of the coercive field in the model gives a thickness of the defect region of the order of 1 nm and demagnetizing field values in excess of 1 T. Still considering that reversal is a nucleation phenomenon (full reversal develops from a very small initial nucleus), Givord *et al.* concluded that various experimental results are not compatible with S-W true nucleation. They suggested the occurrence of a propagation/expansion mechanism, reminiscent of domain wall de-pinning, with thermal activation playing an important role^{5,6}.

The angular dependence of the coercive field constitutes an important tool to identify the processes governing magnetization reversal in hard magnetic materials. Theoretical models for the angular dependence of the coercive field H_c include the Stoner-Wohlfarth (S-W) model $H_c^{SW}(\theta) = H_A(\cos^{2/3}\theta + \sin^{2/3}\theta)^{-3/2}$, based on coherent rotation, where $H_A = 2K_1/\mu_0M_s$ is the anisotropy field, K_1 is the uniaxial magnetocrystalline anisotropy constant and M_s is the saturation magnetization and the Kondorsky model $H_c^K(\theta) = H_p/\cos\theta$, which was originally derived through consideration of pinning mechanisms at internal defect sites, where H_p is the field required to depin a domain wall from the defects (it is implicitly assumed here that $H_p \ll H_A$). Various experimental studies considered the angular dependence of the coercive field in Nd₂Fe₁₄B magnets^{3,7-10}. A difficulty in the experimental analysis is the fact that angular dependence of the coercive field is substantially flattened by the distribution of easy-axis orientation in real magnets⁸⁻¹¹. In the case where reversal is governed by S-W nucleation, further flattening of the angular dependence of the coercive field can be linked to the reduced influence of defects on the nucleation field at large angles¹¹.

Recent numerical evidence from atomistic calculations for Nd₂Fe₁₄B sintered magnets¹² suggest that this defect thickness varies between 0.4 nm and 1.6 nm. It is also possible that the ground boundary phase itself is weakly ferromagnetic and acts as a soft defect at the surface of the Nd₂Fe₁₄B grains.¹³

In this work, the polyhedral grains in Nd₂Fe₁₄B magnets will be approximated by a

cube model. In such polyhedral magnetic grains reversal begins at the edges, usually a corner, where increased demagnetizing field causes localized curling of the magnetization. The magnetization reversal process will be computed numerically by solving the equation of motion for the magnetization. As opposed to linearized micromagnetic models⁷ both the linear and non-linear nature of the equations will be taken into account. Demagnetizing fields will cause a non-uniform magnetization in the remanent state^{14,15}, thus requiring to redefine the classical term “nucleation field”. We will show that two distinct fields can be defined: The critical field that leads to a reversed nucleus at the corner and the critical field at which the nucleus expands. This result from dynamic micromagnetic simulations will be confirmed by numerically computing the energy barrier for magnetization switching. At the saddle point the magnetization is already reversed near the corner. Thermal activation of a further increase of the external field will cause an expansion of the reversed nucleus. The angular dependence of the coercive field will then be compared to experimental data.

In a layered nanocomposite magnet there are three critical fields to consider; the nucleation field H_n^{soft} of the soft layer, the nucleation field H_n^{hard} of the hard layer, and the field H_p required to depin a fully developed or partial domain wall from the boundary between the soft and the hard phase. At nucleation the magnetization starts to deviate from the c axis and a partial domain wall, within which the magnetization rotates less than 180° , forms. If a defect region with severely reduced uniaxial anisotropy (e.g. $K_1^{\text{soft}} = 0$) is present, H_n^{soft} and H_p are always lower than H_n^{hard} , so the overall coercive field is determined by Eq. (1).

$$H_c = \max(H_n^{\text{soft}}, H_p) \quad (1)$$

Aharoni¹⁶ gives analytical expressions for the nucleation field and coercive field for a one-dimensional micromagnetic model, an infinite material with a finite slab of certain thickness and $K_1 = 0$. In a two-phase magnet with a main hard phase and a soft layer of finite thickness t , H_n^{soft} can be analytically estimated from Eq. (2) as long as t is larger than the hard phase domain wall width δ_{hard} .^{17,18} Generally, decreasing the soft layer thickness increases the nucleation field.

$$H_n^{\text{soft}} = \frac{2K_1^{\text{soft}}}{\mu_0 M_s^{\text{soft}}} + \frac{2A^{\text{soft}}\pi^2}{4t^2\mu_0 M_s^{\text{soft}}} \quad (2)$$

where M_s^{soft} is the saturation magnetization and A^{soft} is the exchange constant, both of the soft material.

The pinning field H_p for a domain wall at the interface between a soft and hard layer, after some simplifications, can be calculated from Eq. (3).^{19,20}

$$H_p = \frac{1}{4} \times \frac{2(K_1^{\text{hard}} - K_1^{\text{soft}})}{\mu_0 M_s^{\text{soft}}} \quad (3)$$

where K_1^{hard} and K_1^{soft} are the uniaxial anisotropy constants in the hard phase and soft phase respectively. Thus, assuming the magnet to behave as an exchange-spring and with $K_1^{\text{soft}} = 0$ we can account for a 75% reduction of H_p with respect to the anisotropy field $H_A = 2K_1^{\text{hard}}/\mu_0 M_s^{\text{hard}}$, the theoretical coercive field of the hard phase alone. Material parameters for Nd₂Fe₁₄B at room temperature were obtained from the literature as $K_1 = 4.8 \text{ MJ/m}^3$, $\mu_0 M_s = 1.59 \text{ T}$ and $A = 7.6 \text{ pJ/m}$.^{21,22} For these material parameters, the interfacial depinning field is $\mu_0 H_p = 1.90 \text{ T}$. The domain wall width for the hard material is $\delta_{\text{hard}} = \pi\sqrt{A/K_1} = 3.95 \text{ nm}$.

In this work we consider a single-grain model of cubic geometry with sides $L = 100 \text{ nm}$ and a shell-like defect region in one corner only which allows us to locally use a fine mesh for sufficient accuracy (Fig.1). The defect shell has thickness t and forms a right-angle triangle on each of the three incident cube faces, with adjacent and opposite sides measuring $s = 30 \text{ nm}$. For Eq. (2) to be applicable, the domain wall nucleated in the corner of the cube model has to fit into the diagonal space between the outer and inner corners of the defect so the minimum shell thickness that can fully accommodate a domain wall is $t_{\text{min}} = \sqrt{\delta_{\text{hard}}^2/3} = 2.28 \text{ nm}$. In the defect region we assume $K_1 = 0$ while M_s and A remain identical to the values in the hard phase. The finite element method is used to numerically solve the Landau-Lifschitz-Gilbert (LLG) equation. At each time step we apply a hybrid finite element/boundary element method to compute the magnetic scalar potential.²³ A fine mesh is used in the tetrahedral region near the corner so the nucleus and the partial domain wall are located within the fine region before and after depinning. Mesh size is constrained by the geometry of the defect, but in all models the maximum element edge size in the fine mesh region is 1.0 nm , below any critical lengths of the materials.²³ Elsewhere, a coarse mesh size of 10 nm is sufficient. The magnet is initially saturated along $+z$ and allowed to relax to its remanent state. An external magnetic field H is applied in the opposite direction at a certain field angle θ from the $-z$ axis in the $x - y$ plane. The magneto-crystalline anisotropy axis is oriented parallel to z . The field strength is ramped up slowly enough (much slower than the speed of the Larmor procession for the material,²⁴) so that

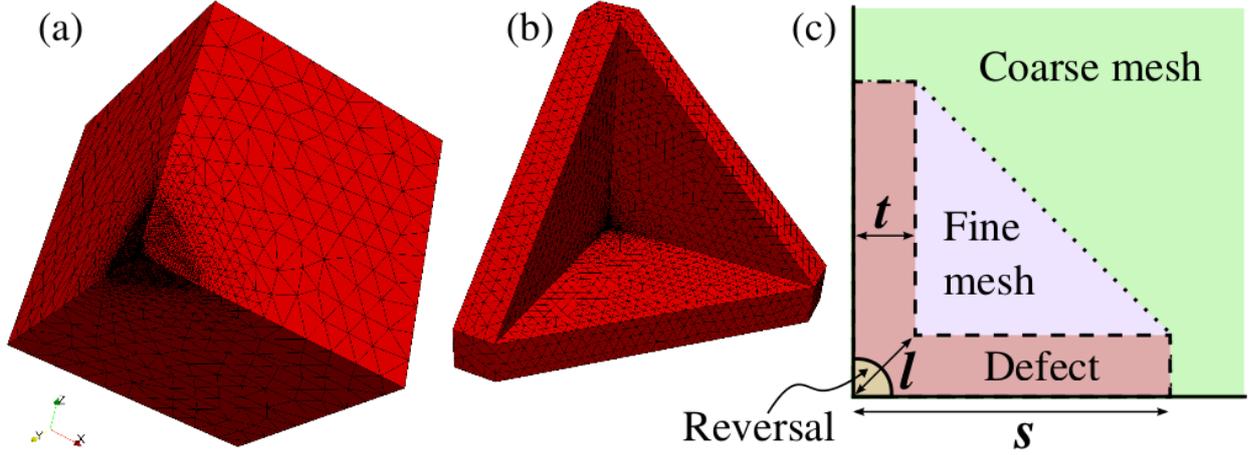


FIG. 1. (a) The single grain model is geometrically a $L \times L \times L$ cube with a defect shell confined to one corner. (b) The defect shell (seen here from the inside) has thickness t and edge size s , measured along the cube edges. (c) A 2D schematic of the defect corner geometry shows the location of increased finite element mesh density, which includes the defect and extends into the hard phase, filling the concave defect cavity. A reversal domain expands from the outer corner of the defect, growing inwards.

each intermediate state can be considered an equilibrium state. H_n is taken to be the field required to flip the polarity of the z -component of the magnetization M_z at the very corner of the cube, which corresponds to formation of at least a 90° domain wall at that corner. H_c is measured as the instantaneous external field value at the moment when the centre of the reversal domain wall reaches the edge of the fine mesh region, since the rapid expansion of the reversal domain is extremely fast while the field strength changes extremely slowly. To find the saddle-point for a specific reversal the nudged elastic band (NEB) method is used to minimize the energy path, taking input from the initial LLG simulations.²³ A series of NEB simulations can be used to calculate the energy barrier height as a function of H , and fitting to Sharrock's law²⁵ it is possible to estimate H_c at a barrier height of $25kT$, which corresponds to room-temperature stability when an attempt frequency of $f_0 = 10^{10}$ Hz is assumed.

The angular dependency of coercivity is measured experimentally for four different hot-deformed nano-crystalline NdFeB samples, where a NdCu grain boundary infiltration process has been applied. A piece of eutectic NdCu alloy is placed on top of the nano-crystalline

base material sample and the system is annealed at 600° C. This increases the volume fraction of the Nd-rich intergranular boundary phase, increasing coercivity and reducing the remanent magnetization.¹³ The four samples consist of the base material (no infiltration) and 5%, 10% and 20% infiltration, where these percentages are expressed in terms of outer mass percentage against mass of base materials. By infiltration treatment, we have confirmed there is no change in texture degree and grain size. The samples have parallelepiped geometry with average dimensions $5 \times 5 \times 0.5 \text{ mm}^3$. After saturation they are rotated about an angle θ (0° to 85°) from the c axis and the field direction is inverted in order to measure the demagnetization curve using a superconducting quantum interference device vibrating sample magnetometer (SQUID-VSM). All measurements are made at a temperature of 300 K. The coercive field H_c for each angle is taken at the maximum value of $dM(\theta)/dH(\theta)$.

Fig.2 contains a plot and visualizations of the computed reversal for both a grain with shell thickness $t = 1.6 \text{ nm}$ and $t = 0.0 \text{ nm}$ (i.e. no defect) with $\theta = 0^\circ$. In both cases the edge inhomogeneities, focussed at the cube corner, are the focal points of initial internal rotation, since the effective field angle is locally reduced. This is followed by the nucleation of a reversal domain at the very corner of the cube inside the defect. In the defect model a defect-mediated nucleation of a reversal domain inside the shell occurs at an external field strength $\mu_0 H_n = 1.69 \text{ T}$ (B). The reversal domain may then expand up to the defect limit, where further expansion is inhibited by an energy barrier. At the de-pinning field $\mu_0 H_p = 2.0 \text{ T}$ (C) this energy barrier is overcome, leading to rapid expansion (D) and eventually reversal of the whole grain. In the defect-free case, the field required for nucleation is much higher at 5.8 T (G), so internal rotation continues until a much higher field. We note that full reversal of the defect-free cube does not proceed by rotation alone.

Fig. 3a contains a plot of the saddle-point magnetization components along the inner diagonal from the corner for $t = 1.6 \text{ nm}$ and $\theta = 0^\circ$. At the moment of de-pinning the reversal domain already extends past the defect and has entered into the main hard phase.

Fig. 3b contains a plot of the computed H_n and H_c against t . These two field values becomes closer with smaller t until they converge. For larger t , $H_c > H_n^{\text{soft}}$ so, as per Eq. (1) it is concluded that $H_c = H_p$. Likewise, for small t below the convergence value it is concluded that $H_c = H_n$. Theoretical plots are included from Aharoni's 1-dimensional nucleation theory for a domain wall in defects.¹⁶ The equations have been rescaled by $3/4$ to consider the cubic geometry, so that $\mu_0 H_a = 5.81 \text{ T}$.²⁶ Theoretically, the maximum reduction in H_c

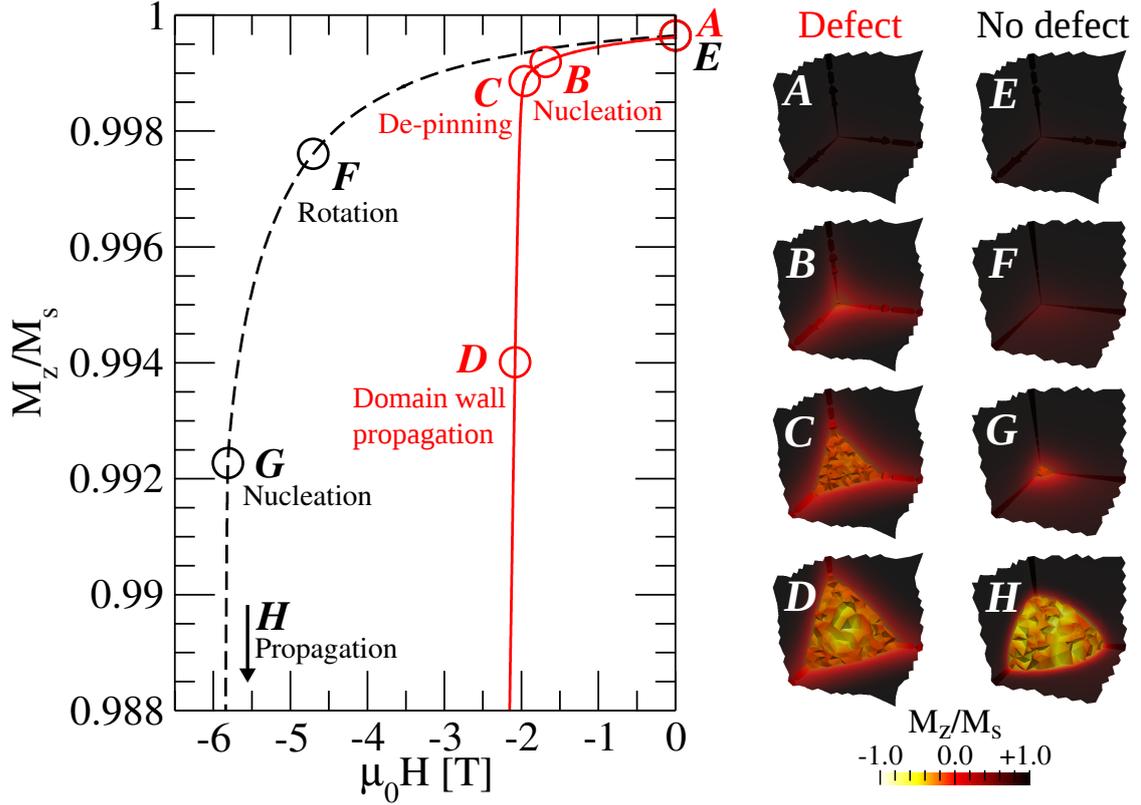


FIG. 2. Reversal process for both the cube model with a defect shell thickness $t = 1.6$ nm and that with no defect shell. $M - H$ reversal curves for both cases show distinct nucleation and pinning mechanisms.

in an exchange spring magnet can be achieved with a soft layer of $l = \sqrt{2\pi^2 A^{\text{soft}}/K_1^{\text{hard}}}$, corresponding to $l = 5.59$ nm and $t = \sqrt{l^2/3} = 3.23$ nm for our material.²⁷ This is in excellent agreement with Fig. 3b, where above a shell thickness of approximately $t = 3$ nm H_c converges to 1.38 T.

Fig. 4 contains absolute and normalized plots of the computed $H_c(\theta)$ for various t , the experimental data for varying infiltration percentage and the theoretical S-W and Kondorsky plots for comparison, where for the Kondorsky plot we use $H_c(0) = H_p$, from Eq. (3) and where, in order to replicate the effects of grain misalignment, we apply a simple modification rule to the simulated and theoretical data: for each field angle θ the corresponding H_c value is replaced by the lowest value within a certain angular range $\pm\delta$. A value of $\delta = 15^\circ$ is chosen to match the angular distribution measured in the experimental samples.¹³ This adjustment flattens the minimum to a plateau and reduces H_c overall, giving similar results

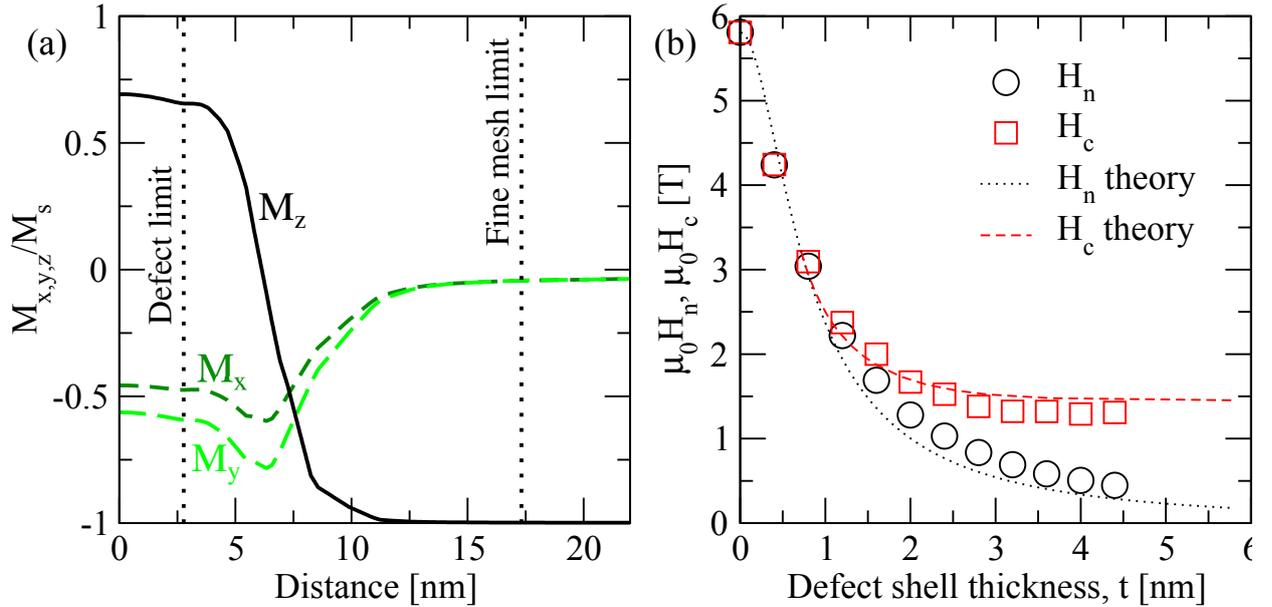


FIG. 3. (a) Plot of the saddle-point M_x , M_y and M_z magnetization components along a diagonal from the reversal corner towards the opposite corner of the cube. The data is taken from the saddle-point configuration of a nudged elastic band (NEB) simulation, which is the highest energy magnetization configuration in the energy-minimized reversal path. (b) A plot of $\mu_0 H_n$ and $\mu_0 H_c$ against defect thickness t , with Aharoni's 1D defect model for comparison.

to the one described in⁸⁻¹⁰ where the angular dependence was calculated for an assembly of imperfectly-oriented exchange-decoupled grains. As the value of t increases, a shift to Kondorsky-like behavior is seen, with the minima shifting to lower angles and becoming increasingly less pronounced, which is demonstrative of the increased importance of the defect-driven nucleation. Above a value of $t = t_{\min}(= 2.28 \text{ nm})$, where a full domain wall width is able to fit into the soft layer, the computed plots converge. From the experimental data, the base material shows the lowest H_c , which becomes larger with increased NdCu infiltration. With infiltration treatment, we confirmed no change in both degree of texture and grain size as described before, so that we can control the structure of the grain boundary. For the base material a Kondorsky-like angular dependence is clearly observed, whereas, with greater infiltration increasing similarity to S-W behavior can be seen, with a weak minimum below 45° .

The progressive shift, from Kondorsky-like to more coherent-rotation like behaviour, may be linked to the associated increase in coercivity^{9,10} from non-infiltrated to infiltrated mag-

nets. This increase itself can be attributed to two possible phenomena. First, the NdCu infiltration may modify the magnetism of the weakly-ferromagnetic intergrain boundary or second, it may reduce surface distortion and weaken the disordered surface defect of reduced anisotropy at the interface between the $\text{Nd}_2\text{Fe}_{14}\text{B}$ grains and the intergrain boundary.

Experimental results seem to be lower in magnitude than simulation but a direct comparison is not possible since the defect thicknesses of the experimental samples are unknown. By increasing further the defect thickness, the coercive field does not decrease much further. The presence of a graded interface between the hard phase and the soft defect is also likely to be important. Furthermore, thermal activation, which was not considered in the simulations, will reduce coercivity at non-zero temperature.²³ At 300 K H_c was typically reduced by up to 20 %.

The results presented here provide compelling evidence that the angle-dependent coercivity behavior of NdFeB magnets is determined by soft defects at the boundaries between the main NdFeB grains. Using a simple adjustment of the single grain results to replicate the behavior in bulk samples, where there are many grains and an angular distribution in their anisotropy angles, we have been able to reproduce the behavior seen experimentally and find close agreement with the predictions from simple analytical models of soft defects. Recently, a weakly ferromagnetic grain boundary phase in $\text{Nd}_2\text{Fe}_{14}\text{B}$ based magnets was reported.¹³ One of the possibilities that explains the angular dependence of coercivity, which we have simulated by assuming the presence of a surface defect as a magnetically soft phase, is that a weakly-ferromagnetic boundary phase may itself act as a surface defect for the neighboring $\text{Nd}_2\text{Fe}_{14}\text{B}$ grain. Thus the micromagnetic model presented in this paper would still be applicable. At this moment, the authors are investigating the existence of disordered surface defects and their thicknesses. This should make clear which is the dominant factor for angular dependence of coercivity; the disordered surface defect or the possible weak ferromagnetism of the grain boundary phase.

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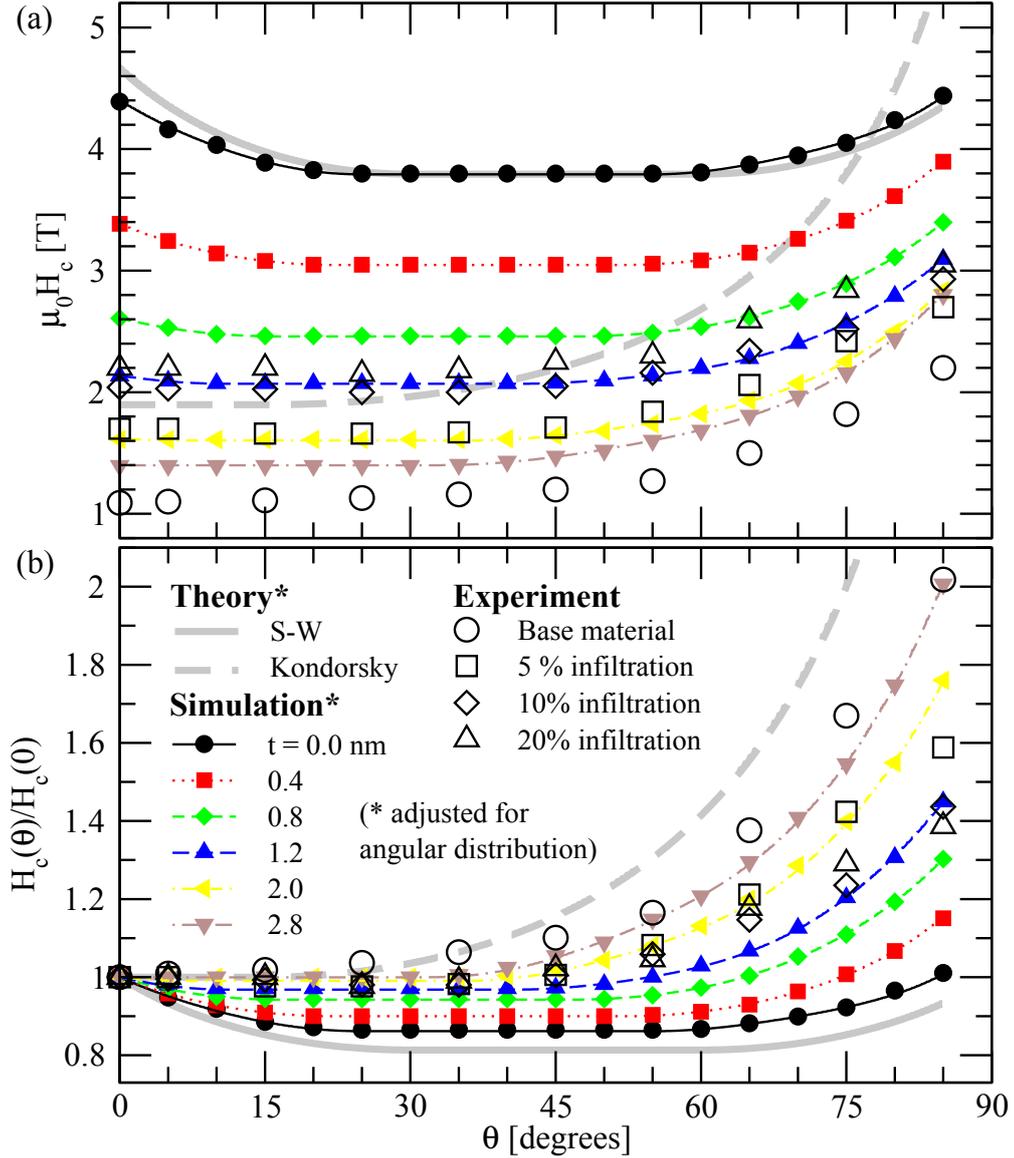


FIG. 4. (a) Simulation results for angular dependence of coercive field $\mu_0 H_c$ for Nd₂Fe₁₄B at temperature $T = 300$ K with varying defect shell thickness t and experimental data for the four samples of varying NdCu infiltration. (b) The same data with normalized units. Theoretical plots for the Stoner-Wohlfarth (S-W) and Kondorsky pinning (dashed line) models are given for comparison. A simple adjustment to the simulated and theoretical plots has been made to replicate the 15° angular distribution observed in the experimental samples.